



# HYDRAULIC FLUID FLOW AND PRESSURE THEORY

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# COMPRESSIBILITY

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For simple hydraulic design it can be assumed oil is incompressible, however the compressibility and density of oil is a factor in sophisticated hydraulic components. Bulk modulus is a measure of incompressibility. The higher the bulk modulus the less compressible or stiffer the fluid.

Mathematically the bulk modulus is defined by  $\beta = -V\left(\frac{\Delta P}{\Delta V}\right)$  where:  $\beta$  = bulk modulus (psi)  
 $V$  = original volume (in.<sup>3</sup>)  
 $\Delta P$  = change in pressure (psi)  
 $\Delta V$  = change in volume (in.<sup>3</sup>)

The bulk modulus of an oil changes somewhat with pressure and temperature, but within the operating ranges in most fluid power systems, this factor can be neglected. A typical value for oil is 250,000 psi.

## EXAMPLE:

A 10-in.<sup>3</sup> sample of oil is compressed in a cylinder until its pressure is increased from 100 to 2000 psi. If the bulk modulus equals 250,000 psi. find the change of volume of the oil.

**SOLUTION:** To solve for  $\Delta V$ , we have:  $\Delta V = -V\left(\frac{\Delta P}{\beta}\right) = -10\left(\frac{1900}{250,000}\right) = -0.076 \text{ in.}^3$

This represents only a 0.76% decrease in volume, which shows that the oil is highly incompressible.

# PRESSURE WAVES

Another important consequence of the compressibility of fluids is that disturbances introduced at some point in the fluid propagate at a finite velocity. For example, if a fluid is flowing in a pipe and a valve at the outlet is suddenly closed (thereby creating a localized disturbance) the effect of the valve closure is not felt instantaneously upstream. It takes a finite time for the increased pressure created by the valve closure to propagate to an upstream location. The speed of sound or the speed of a pressure wave in oil is approximately 4200 feet per second. The speed of sound varies with temperature and density. The following are typical wave speeds for comparative purposes only:

<b>SPEED OF SOUND IN OIL</b>	<b>4200 FEET PER SECOND</b>
<b>SPEED OF SOUND IN WATER</b>	<b>4780 FEET PER SECOND</b>
<b>SPEED OF SOUND IN AIR</b>	<b>1200 FEET PER SECOND</b>
<b>SPEED OF LIGHT</b>	<b>186,000 MILES PER SECOND</b>